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Effects of New Goods and Product Turnover on Price Indexes^{*}

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Abstract

This study analyzes the importance of new products for price measurements. Using large-scale retail scanner data in Japan, we construct a unit value price index and decompose its fluctuation into (1) standard price change effects, (2) substitution effects within continuing goods, and (3) turnover-new product effects. The aggregate unit price index exhibits different movements from the standard Laspeyres price index. After the 2014 change in Japan's tax rate, turnover-new product effects from the appearance of relatively expensive new goods increased by 1 percentage point, contributing to increases in unit value. However, the standard Laspeyres price index, which excludes information for new or disappearing goods, exhibited no large changes before and after the tax revision.

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1. Introduction

Establishing how the entry and exit of commodities affect cost of living indexes is a serious econometric problem. Most countries' official consumer price indexes (CPI) are based on fixed bundles of commodities that exist both in the base and current periods. For each commodity category such as pasta or milk, typically, only one or a few specific brands is adopted in the bundles. In the real economy, hundreds of different pasta and milk brands are traded. More importantly, new products are introduced into markets almost daily, and a significant numbers of goods disappear.

Although official CPIs are based on a limited number of products, economic data such as consumer expenditures and company sales cover all products that are traded. That is, the price index is based on continuing goods, while expenditure data include new goods that just enter markets. This divergence in product space between expenditures and the price index could cause serious measurement problems if the new goods are priced differently from incumbent goods.

Figure 1 shows the weekly appearance rate in Japan of new products in supermarkets, convenience stores, general merchandise stores, and drug stores.¹ More precisely, it shows the ratio of the number of products that did not exist during the same week in the previous year to total products.² Measured by sales, new products are about 35% of all products. Accordingly, by limiting the product bundle to products that remain in the market for more than one year, a significant quantity of sales information is neglected.

¹ Section 3 describes the data in detail.

² Figure 1 treats goods with identical commodity codes (Japanese Article Number: JAN) sold at different stores as different commodities. Therefore, the product appearance rate does not necessarily correspond to the appearance rate of new product brands.

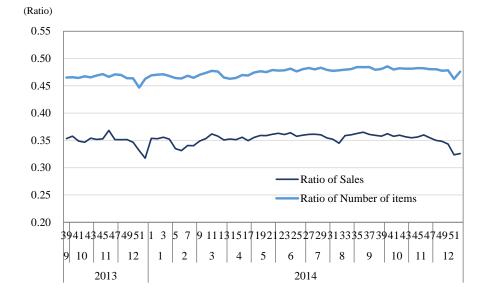


Figure 1: Product Appearance Rate

Notes: The ratios of sales and the number of items. Numerators are the sales or the number of items sold in the current period but not sold during that week one year earlier. Denominators are total sales or the total number of items sold in the current period. When constructing ratios, we calculated the ratios at store level, and then, aggregated over stores.

If prices of new products were not systematically different from those of incumbent goods, neglecting new products would not raise serious problems when estimating price indexes. Unfortunately, this is not the case. Figure 2 compares prices of new and old products. The line shows the relative (unit) price of newly introduced cup noodles to incumbent cup noodles. Soon after the introduction of the new cup noodles, the price tends to be about 20% higher than that of the incumbent goods.³ That is, prices of new goods exceed prices of incumbent goods.⁴ How important are new products for price measurement? This study addresses that issue.

 ³ Pricing patterns over product life cycles and their relations to price indexes are an active research area. See Balk (2000), Klenow (2003), Bils (2009), and, Melser and Syed (2013), for examples.
 ⁴ Of course, new products might have higher quality, which would reduce their "real" prices. Since

⁴ Of course, new products might have higher quality, which would reduce their "real" prices. Since the quality of processed foods and daily necessities is very hard to measure, the treatment of product-level quality changes of this paper is limited to changes in physical volume only. That is, this paper does not consider changes in tastes or packages.

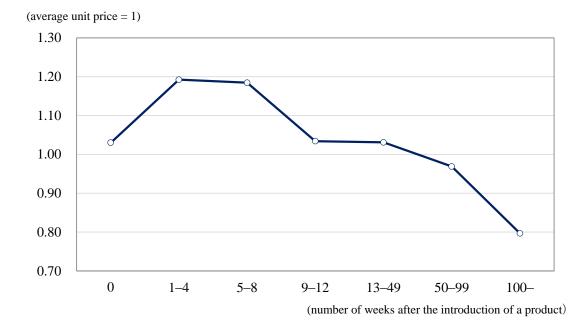


Figure2: Difference in Unit Prices of New and Old Cup Noodles

Notes: Relative price of items classified as cup noodles that are traded during September 2012 and December 2014. The horizontal axis shows the number of weeks passed after introduction of the items. The vertical axis is the relative price of the items. The average price normalizes at unity. Relatively low prices in Week 0 might reflect bargain sales to promote new goods.

The treatment of new products is a central issue in constructing price indexes. An entire chapter of the CPI Manual discusses quality adjustment methods for new products using hedonic and overlap approaches.⁵ Based on a constant-elasticity-of-substitution (CES) aggregator function, Feenstra (1994) and Feenstra and Shapiro (2003) derive a formula for a true cost-of-living index that the variety of products required for living changes over time. Also based on CES aggregator function, Broda and Weinstein (2010) find that new goods cause a significant "bias". Broda and Weinstein (2010) assume the market share of each commodity reflects its quality. This study does not assume any specific functional form for utility or expenditure functions. Rather, to evaluate the contribution of new and disappearing goods, we extend the decomposition technique developed by Silver (2009, 2010) and Diewert and Lippe (2010). Although Silver (2009, 2010) and Diewert and Lippe (2010). Although Silver (2009, 2010) and Diewert and Lippe (2010) to vary over time, we include changes in variety and derive a simple decomposition formula that is easy to calculate. In particular, we decompose changes in the unit value price index into changes in the standard product-level price change within continuing goods, the substitution effects within continuing goods, and the turnover-new product effects.

⁵ See Chapter 8 of ILO (2004).

The study yields several major findings. The aggregate unit value price index shows a higher rate of inflation than other price indexes such as the Törnqvist Index. Product turnover effects are generally positive, implying that new products are priced higher than disappearing or continuing goods. Substitution effects are generally negative, implying that volume shares and prices have negative correlation. When large macroeconomic shocks occur, the two effects move differently. Japan's consumption tax increased from 5% to 8% in April, 2014, its first major change since 1997. Immediately before the tax change, the substitution swelled, likely reflecting consumer stockpiling behavior that caused the unit value price inflation to drop substantially. On the other hand, changes in price effects measured by the Laspeyres formula hardly occurred before or after the tax revision, which implies that the product-level pricing behaviors remained unchanged during the sample period. We also observe that after the increase in the tax rate, turnover-new product effects from the appearance of relatively expensive new goods increased by 1 percentage point, which contributed to the increase in unit value prices.

This paper proceeds as follows. Section 2 explains how the unit price index can be decomposed into three price change effects. Section 3 describes scanner data used in this study. Section 4 discusses both aggregate and category-level results of our decomposition. Finally, Section 5 presents the conclusions to this study.

2. Price Index Decomposition

In this section, we explain the procedure to decompose changes in the unit value price index into changes in the standard product-level price change within continuing goods, the substitution effects within continuing goods, and the turnover-new product effects.

We define variables as follows; Θ_t : set of all items of category Θ in period *t*, C_t : set of items in category Θ sold both in periods *t* and t - y, N_t : set of items in category Θ sold in period *t* but not in period t - y, O_t : set of items in category Θ not sold in period *t* but sold in period t - y, q_t^i : quantity of item *i* sold in period t, $^6 p_t^i$: price of item *i* sold in period *t*. We call commodity that belong to the set N_t , O_t , and C_t as new goods, disappearing goods, and continuing goods, respectively.

⁶ This study measures prices and quantities for each product category in a common unit, such as price per milliliter. In actual scanner data, commodity-level data have unique volume information (v)—e.g., product A's price is ¥300 per milliliter. We transform the original price and quantity information into unit value price and quantity as follows: price = original_price/v, quantity = original_quantity $\times v$.

Then, the quantity-weighted average unit value price in period $t(P_t^{\Theta})$ can be expressed as the weighted sum of the unit value price of continuing goods (P_t^C) and new goods (P_t^N) .

$$P_t^{\theta} \equiv \sum_{i \in \Theta_t} \left[\left(\frac{q_t^i}{\sum_{j \in \Theta_t} q_t^j} \right) p_t^i \right]$$
$$= \sum_{i \in C_t} \left[\left(\frac{q_t^i}{\sum_{j \in \Theta_t} q_t^j} \right) p_t^i \right] + \sum_{i \in N_t} \left[\left(\frac{q_t^i}{\sum_{j \in \Theta_t} q_t^j} \right) p_t^i \right]$$
$$= \left(\frac{\sum_{j \in C_t} q_t^j}{\sum_{j \in \Theta_t} q_t^j} \right) \sum_{i \in C_t} \left[\frac{q_t^i}{\sum_{j \in C_t} q_t^j} \times p_t^i \right] + \left(\frac{\sum_{j \in N_t} q_t^j}{\sum_{j \in \Theta_t} q_t^j} \right) \sum_{i \in N_t} \left[\left(\frac{q_t^i}{\sum_{j \in N_t} q_t^j} \right) p_t^i \right]$$
$$= w_t^C P_t^C + w_t^N P_t^N,$$
(1)

where
$$w_t^C = \frac{\sum_{j \in C_t} q_t^j}{\sum_{j \in \Theta_t} q_t^j}, w_t^N = \frac{\sum_{j \in N_t} q_t^j}{\sum_{j \in \Theta_t} q_t^j}, P_t^C = \sum_{i \in C_t} \left[\frac{q_t^i}{\sum_{j \in C_t} q_t^j} \times p_t^i \right], P_t^N = \sum_{i \in N_t} \left[\left(\frac{q_t^i}{\sum_{j \in N_t} q_t^j} \right) p_t^i \right].$$

Note that, by construction, $w_t^N = 1 - w_t^C$.

Similarly, we can construct the unit value price index in period t - y as the weighted sum of the unit value prices of continuing and disappearing goods.

$$P_{t-y}^{\theta} = \sum_{i \in \theta_{t-y}} \left[\left(\frac{q_{t-y}^{i}}{\sum_{j \in \theta_{t-y}} q_{t-y}^{j}} \right) p_{t-y}^{i} \right]$$

$$= \left(\frac{\sum_{j \in C_{t}} q_{t-y}^{j}}{\sum_{j \in \theta_{t}} q_{t-y}^{j}} \right) \sum_{i \in C_{t}} \left[\frac{q_{t-y}^{i}}{\sum_{j \in C_{t}} q_{t-y}^{j}} \times p_{t-y}^{i} \right] + \left(\frac{\sum_{j \in O_{t}} q_{t-y}^{j}}{\sum_{j \in \theta_{t}} q_{t-y}^{j}} \right) \sum_{i \in O_{t}} \left[\frac{q_{t-y}^{i}}{\sum_{j \in O_{t}} q_{t-y}^{j}} \times p_{t-y}^{i} \right]$$

$$= w_{t-y}^{C} P_{t-y}^{C} + w_{t-y}^{O} P_{t-y}^{O},$$
where $w_{t-y}^{C} = \frac{\sum_{j \in C_{t}} q_{t-y}^{j}}{\sum_{j \in \theta_{t}} q_{t-y}^{j}}, w_{t-y}^{O} = \frac{\sum_{j \in O_{t}} q_{t-y}^{j}}{\sum_{j \in \theta_{t}} q_{t-y}^{j}},$

$$P_{t-y}^{C} = \sum_{i \in C_{t}} \left[\frac{q_{t-y}^{i}}{\sum_{j \in C_{t}} q_{t-y}^{j}} \times p_{t-y}^{i} \right] \quad \text{and} P_{t-y}^{O} = \sum_{i \in O_{t}} \left[\frac{q_{t-y}^{i}}{\sum_{j \in O_{t}} q_{t-y}^{j}} \times p_{t-y}^{i} \right].$$

$$(2)$$

The inflation rate of the unit price index, $\pi_t^{\theta} (\equiv \frac{P_t^{\theta} - P_{t-y}^{\theta}}{P_{t-y}^{\theta}})$, can be written as follows:

$$\pi_{t}^{\theta} \equiv \frac{P_{t}^{\theta} - P_{t-y}^{\theta}}{P_{t-y}^{\theta}}$$

$$= \frac{w_{t}^{C} P_{t}^{C} - w_{t-y}^{C} P_{t-y}^{C}}{P_{t-y}^{C}} \frac{P_{t-y}^{C}}{P_{t-y}^{\theta}} + \frac{w_{t}^{N} P_{t}^{N} - w_{t-y}^{0} P_{t-y}^{0}}{P_{t-y}^{0}} \frac{P_{t-y}^{0}}{P_{t-y}^{\theta}}$$
(3)

$$=w_{t-y}^{C}\frac{(w_{t}^{C}/w_{t-y}^{C})P_{t}^{C}-P_{t-y}^{C}}{P_{t-y}^{C}}\left(\frac{P_{t-y}^{C}}{P_{t-y}^{\Theta}}\right)+w_{t-y}^{O}\frac{(w_{t}^{N}/w_{t-y}^{O})P_{t}^{N}-P_{t-y}^{O}}{P_{t-y}^{O}}\left(\frac{P_{t-y}^{O}}{P_{t-y}^{\Theta}}\right)$$

We can rewrite this equation as:

$$\pi_t^{\Theta} = w_{t-y}^C \,\hat{\pi}_t^C \left(\frac{P_{t-y}^C}{P_{t-y}^{\Theta}} \right) + w_{t-y}^O \hat{\pi}_t^T \left(\frac{P_{t-y}^O}{P_{t-y}^{\Theta}} \right),\tag{4}$$

where $\hat{\pi}_{t}^{c} \equiv \frac{(w_{t}^{C}/w_{t-y}^{C})P_{t}^{C}-P_{t-y}^{C}}{P_{t-y}^{C}}$ and $\hat{\pi}_{t}^{T} \equiv \frac{(w_{t}^{N}/w_{t-y}^{O})P_{t}^{N}-P_{t-y}^{O}}{P_{t-y}^{O}}$.

 $\hat{\pi}_t^T$ can be decomposed into three effects, (1) the changes in weights of new and disappearing goods, $(w_t^N/w_{t-y}^O - 1)$, (2) the price differential between new and disappearing goods (π_t^{NO}) , and (3) the cross term as follows:

$$\hat{\pi}_{t}^{T} = \frac{\left(w_{t}^{N}/w_{t-y}^{O}\right)P_{t}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}$$

$$= \left(w_{t}^{N}/w_{t-y}^{O} - 1\right)\frac{P_{t}^{N}}{P_{t-y}^{O}} + \frac{P_{t}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}$$

$$= \left(w_{t}^{N}/w_{t-y}^{O} - 1\right)(1 + \pi_{t}^{NO}) + \pi_{t}^{NO}$$

$$= \left(w_{t}^{N}/w_{t-y}^{O} - 1\right) + \pi_{t}^{NO} + \left[\left(w_{t}^{N}/w_{t-y}^{O} - 1\right)\pi_{t}^{NO}\right],$$

$$= P_{t-y}^{O}$$
(5)

where $\pi_t^{NO} \equiv \frac{P_t^N - P_{t-y}^O}{P_{t-y}^O}$.

The inflation rate of continuing goods, π_t^{CL} , can be written as

$$\pi_t^{CL} = \frac{\ddot{P}_t^C - P_{t-y}^C}{P_{t-y}^C} = \frac{\sum_{i \in C_t} \left[\frac{q_{t-y}^i}{\sum_{j \in C_t} q_{t-y}^j} \times p_t^i \right] - \sum_{i \in C_t} \left[\frac{q_{t-y}^i}{\sum_{j \in C_t} q_{t-y}^j} \times p_{t-y}^i \right]}{\sum_{i \in C_t} \left[\frac{q_{t-y}^i}{\sum_{j \in C_t} q_{t-y}^j} \times p_{t-y}^i \right]} = \frac{\sum_{i \in C_t} \left[q_{t-y}^i p_t^i \right]}{\sum_{i \in C_t} \left[q_{t-y}^i p_{t-y}^i \right]} - 1,$$
(6)
where $\ddot{P}_t^C = \sum_{i \in C_t} \left[\frac{q_{t-y}^i}{\sum_{j \in C_t} q_{t-y}^j} \times p_t^i \right],$

which is equivalent to the inflation rate measured by the Laspeyres price index.

To interpret the term with $\hat{\pi}_t^c$, we introduce variables $\tilde{\pi}_t^c$ and ϕ_t^c as follows:

Therefore, we get,

$$\hat{\pi}_{t}^{C} = \left(w_{t}^{C} / w_{t-y}^{C} - 1 \right) (1 + \pi_{t}^{C}) + \phi_{t}^{C} + \phi_{t}^{C} \pi_{t}^{C} + \pi_{t}^{CL}.$$
(8)

 ϕ_t^c can be interpreted as the substitution effects. – Per Diewert and Lippe (2010) define covariance such as,

$$Cov(x, y) = \frac{1}{T} \sum_{i} (x_i - x^*)(y_i - y^*) = \frac{1}{T} \sum_{i} (x_i)(y_i - y^*).$$
(9)

Then, it is possible to obtain,

$$\phi_t^C = \frac{T_t \text{Cov}(p_t, s_t - s_{t-y})}{P_t^C},$$

where $p_t = [p_t^1, p_t^2, ..., p_t^{T_t}], \ s_t = [s_t^1, s_t^2, ..., s_t^{T_t}], \ s_t^i = \frac{q_t^i}{\Sigma_{j \in C_t} q_t^j}$ (10)

and T_t : #(Θ_t), is the number of products sold at time t.

The R.H.S of Equation 10 is equivalent to the formula derived by Diewert and Lippe (2010).⁷ The interpretation of the covariance term is straightforward. If the price of good *i* exceeds the average price, its volume share is expected to decline. This substitution effect captures the degree of the negative correlation.

 $[\]frac{1}{7}$ See Appendix 1 for the derivation.

Finally, using π_t^{CL} , ϕ_t^C , and additional terms, we can express unit value price inflation as the weighted sum of the three price effects and the cross term.⁸

$$\pi_{t}^{\Theta} = \left(\frac{P_{t-y}^{C}}{P_{t-y}^{\Theta}}\right) w_{t-y}^{C} \pi_{t}^{CL} + \left(\frac{P_{t-y}^{C}}{P_{t-y}^{\Theta}}\right) w_{t-y}^{C} \phi_{t}^{C} + \frac{w_{t-y}^{O} \left(P_{t}^{C} - P_{t-y}^{O}\right) + w_{t}^{N} \left(P_{t}^{N} - P_{t}^{C}\right)}{P_{t-y}^{\Theta}} + \left(\frac{P_{t-y}^{C}}{P_{t-y}^{\Theta}}\right) w_{t-y}^{C} \phi_{t}^{C} \pi_{t}^{C}.$$
(11)

The first of the R.H.S. is the standard price change effect measured by the Laspeyres formula. Note that if there were no product turnover, we would obtain $P_{t-y}^{C} = P_{t-y}^{\Theta}$ and $w_{t-y}^{C} = 1$. Thus, the first term would be equal to the standard rate of price change, π_t^{CL} . The second term represents the substitution effects within continuing goods. The third term shows the contribution of product turnover to the unit price index. The numerator of the third term is the weighted sum of the price differential between (1) new goods and continuing goods and (2) continuing goods and disappearing goods. Note that w_{t-y}^{C} is the ratio of disappearing goods within the total volume sold in period t-y, and $P_t^{C} - P_{t-y}^{O}$ shows the differences between the unit value prices of continuing goods and disappearing goods. Note also that w_t^N is the ratio of new goods in the total volume sold in period t, and that $P_t^N - P_t^C$ shows the differences between unit value prices of new and continuing goods. The third term can be interpreted as the substitution effects through product turnover. The final term represents the cross-effect of substitution effects and product price change effects that are supposed to be of second order.

The aggregate rate of change in the unit value price indexes is obtained via the Törnqvist formula in the following ways:

> The aggregate unit value price change rate:

$$\pi_t^{Total} = \exp\left\{\sum_{\Theta} \left[\frac{1}{2} \left(\frac{s_{t-y}^{\Theta}}{\sum_{\Theta} s_{t-y}^{\Theta}} + \frac{s_t^{\Theta}}{\sum_{\Theta} s_t^{\Theta}}\right) \ln(1 + \pi_t^{\Theta})\right]\right\} - 1,\tag{12}$$

> The aggregate price change effects of continuing goods:

$$\pi_t^{CL,Total} = \exp\left\{\sum_{\Theta} \left[\frac{1}{2} \left(\frac{s_{t-y}^{\Theta}}{\sum_{\Theta} s_{t-y}^{\Theta}} + \frac{s_t^{\Theta}}{\sum_{\Theta} s_t^{\Theta}} \right) \ln\left(1 + \left\{ \left(\frac{P_{t-y}^{C}}{P_{t-y}^{\Theta}} \right) w_{t-y}^{C,\Theta} \pi_t^{CL,\Theta} \right\} \right) \right] \right\} - 1,$$
(13)

> The aggregate substitution effect for continuing goods:

⁸ See Appendix 2 for the derivation.

$$\phi_t^{C,Total} = \exp\left\{\sum_{\Theta} \left[\frac{1}{2} \left(\frac{s_{t-y}^{\Theta}}{\sum_{\Theta} s_{t-y}^{\Theta}} + \frac{s_t^{\Theta}}{\sum_{\Theta} s_t^{\Theta}} \right) \ln\left(1 + \left\{ \left(\frac{P_{t-y}^{C}}{P_{t-y}^{\Theta}} \right) w_{t-y}^{C,\Theta} \phi_t^{C,\Theta} \right\} \right) \right] \right\} - 1, \tag{14}$$

The aggregate turnover-new product effect: \triangleright

$$\pi_{t}^{T,Total} = \exp\left\{\sum_{\theta} \left[\frac{1}{2} \left(\frac{S_{t-y}^{\theta}}{\sum_{\theta} S_{t-y}^{\theta}} + \frac{S_{t}^{\theta}}{\sum_{\theta} S_{t}^{\theta}}\right) \ln\left(1 + \left\{\frac{w_{t-y}^{0,\theta} \left(P_{t}^{C,\theta} - P_{t-y}^{0,\theta}\right) + w_{t}^{N,\theta} \left(P_{t}^{N,\theta} - P_{t}^{C,\theta}\right)}{P_{t-y}^{\theta}}\right\}\right)\right]\right\} - 1,$$
(15)

where s_t^{θ} , $P_{t-y}^{O,\theta}$, $P_{t-y}^{C,\theta}$, $\pi_t^{CL,\theta}$, and $\phi_t^{C,\theta}$ are the sales of category θ in period t, the unit value price of disappearing goods of category Θ at time t-y, the unit value price of continuing goods of category θ at time t-y, the price change effects of continuing goods of category θ at time t, and the pure substitution effects of continuing goods of category Θ at time t.

3. Data

We use Japanese store–level weekly scanner data, known as the SRI,⁹ collected by INTAGE Inc. Sales records in the dataset cover sales of processed foods, daily necessities, and cosmetics and drugs that have JAN codes.¹⁰ The sampled period is between October 2012 and December 2014, which enables us to calculate the yearly rate of price changes between October 2013 and December 2014. The dataset cover various types of stores, such as general merchandise stores (218), supermarkets (1,051), convenience stores (818), drug stores (1,066), and specialized stores, such as liquor shops (639) located across Japan.¹¹ Table 1 gives a detailed description of the dataset used to calculate aggregated unit price indexes.

One noteworthy characteristic of the dataset is its detailed commodity classification. As is shown in the third column of Table 1, commodities are classified into more than 1,000 categories, about seven times larger than the number of classifications adopted by Japanese official statistics. As Diewert and Lippe (2010) stress, when constructing a unit value price index, we must wherever possible avoid aggregation over heterogeneous goods. We expect that the dataset's highly detailed classification helps us to rmitigate the aggregation bias indicated by Diewert and Lippe (2010).

To avoid the sample selection effect when calculating the rate of change of individual product

⁹ SRI is the abbreviation for Japanese "Syakaichosa-kenkyujo Retail Index," which translates as "Retail Index by The Institute of Social Research".
¹⁰ Fresh foods are excluded in the dataset because they lack commodity codes.

¹¹ Values in parentheses are the average number of stores during the sample period.

prices, we limit the store and category space to a range such that stores and product categories exist in both the current week and the same week of the previous year. Furthermore, we use observations with volume information only. After these operations, the average number of stores over the sample periods is reduced from 3,831 to 3,469, and the average number of categories falls from 2,519 to 1,070.

Summary Table	e of SRI Data	ı																
	# of Store	# of Category	Sales (Million Yen)						Ratio o	on Sales Disappering				(Thousand)	<u> </u>	Disappering	Ratio on # of iter	
Week t			T o week t		Cont week t	inuing week t-52	New Goods week t	Goods week t-52	New Goods	Goods	To			inuing	New Goods	Goods	New Goods week t	Goods week t-52
2013/09/30	3,486	1,071	week t 13,317	week t-52 13,682	week t 8,613	week t-52 9,340	4,703	4,342	week t 0.353	week t-52 0.317	period t 6,870	period t-52 6,789	period t 3,674	period t-52 3,674	week t 3,197	week t-52 3,115	week t 0.465	0.459
2013/10/07	3,472	1,070	12,764	13,400	8,197	9,043	4,567	4,357	0.358	0.325	6,782	6,764	3,623	3,623	3,159	3,141	0.466	0.464
2013/10/14 2013/10/21	3,459 3,461	1,071 1,068	13,283 13,413	13,571 13,432	8,649 8,763	9,192 9,063	4,634 4,650	4,379 4,369	0.349 0.347	0.323 0.325	6,862 6,850	6,806 6,763	3,675 3,648	3,675 3,648	3,187 3,202	3,131 3,115	0.464 0.467	0.460
2013/10/21 2013/10/28	3,401	1,066	12,723	13,432	8,703	9,003	4,030	4,305	0.347	0.323	6,842	6,786	3,648	3,658	3,202	3,113	0.467	0.461
2013/11/04	3,463	1,068	13,060	13,030	8,467	8,791	4,594	4,240	0.352	0.325	6,844	6,740	3,633	3,633	3,210	3,107	0.469	0.461
2013/11/11 2013/11/18	3,462 3,455	1,069	12,877 12,810	13,006 13,591	8,335 8,092	8,582 9,063	4,543 4,718	4,424 4,528	0.353 0.368	0.340 0.333	6,829 6,824	6,698 6,809	3,609 3,640	3,609 3,640	3,220 3,183	3,090 3,169	0.472 0.467	0.461 0.465
2013/11/18	3,449	1,067	13,511	13,249	8,762	8,898	4,749	4,351	0.351	0.328	6,887	6,740	3,643	3,643	3,243	3,097	0.471	0.459
2013/12/02	3,484	1,076	13,246	13,429	8,591	9,040 9,555	4,655	4,388	0.351	0.327	6,904	6,801	3,659	3,659	3,245 3,257	3,142	0.470	0.462
2013/12/09 2013/12/16	3,493 3,489	1,070 1,069	13,587 13,423	14,199 14,201	8,810 8,771	9,555	4,777 4,652	4,643 4,577	0.352 0.347	0.327 0.322	7,020 6,980	6,998 6,943	3,763 3,742	3,763 3,742	3,257	3,235 3,201	0.464	0.462 0.461
2013/12/23	3,489	1,065	15,431	16,983	10,317	11,941	5,114	5,042	0.331	0.297	7,357	7,335	4,070	4,011	3,288	3,266	0.447	0.445
2013/12/30 2014/01/06	3,244 3,445	1,063	14,544 11,844	12,759 12,239	9,928	8,750 8,153	4,616 4,191	4,010 4,086	0.317 0.354	0.314 0.334	6,913 6,606	6,692	3,713 3,506	3,522 3,506	3,199 3,099	2,979 3,055	0.463	0.445
2014/01/08	3,445	1,060	12,239	12,239	7,652 7,918	8,367	4,191	4,080	0.354	0.334	6,652	6,562 6,535	3,500	3,523	3,099	3,033	0.409	0.466
2014/01/20	3,424	1,057	12,746	12,580	8,211	8,431	4,535	4,148	0.356	0.330	6,722	6,566	3,555	3,555	3,167	3,011	0.471	0.459
2014/01/27 2014/02/03	3,431 3,432	1,057 1,061	12,489 11,924	12,713 12,374	8,087 7,932	8,508 8,456	4,402 3,992	4,204 3,918	0.352	0.331 0.317	6,676 6,528	6,603 6,525	3,552 3,498	3,552 3,498	3,124 3,030	3,051 3,027	0.468	0.462
2014/02/03	3,432	1,060	13,034	12,374	8,716	8,430	4,319	4,003	0.333	0.309	6,690	6,609	3,498	3,498	3,030	3,027	0.464	0.404
2014/02/17	3,410	1,062	13,345	12,768	8,800	8,803	4,544	3,965	0.341	0.311	6,760	6,574	3,593	3,593	3,166	2,980	0.468	0.453
2014/02/24 2014/03/03	3,398 3,428	1,063 1,065	13,515 13,685	13,436 13,131	8,916 8,912	9,244 9,025	4,599 4,773	4,192 4,106	0.340 0.349	0.312 0.313	6,797 6,838	6,692 6,680	3,639 3,622	3,639 3,622	3,158 3,216	3,053 3,058	0.465	0.456 0.458
2014/03/10	3,426	1,005	13,748	12,881	8,890	8,867	4,858	4,014	0.353	0.312	6,863	6,650	3,611	3,611	3,251	3,039	0.474	0.450
2014/03/17	3,427	1,070	15,014	13,013	9,583	8,982	5,431	4,032	0.362	0.310	6,984	6,664	3,650	3,650	3,335	3,014	0.477	0.452
2014/03/24 2014/03/31	3,428 3,425	1,074	17,268 12,537	13,623 13,299	11,089 8,139	9,443 8,914	6,178 4,397	4,180 4,385	0.358 0.351	0.307 0.330	7,279 6,698	6,833 6,756	3,814 3,582	3,814 3,582	3,466 3,115	3,019 3,173	0.476	0.442 0.470
2014/04/07	3,427	1,070	11,319	12,989	7,329	8,529	3,990	4,460	0.352	0.343	6,504	6,767	3,493	3,493	3,011	3,274	0.463	0.484
2014/04/14	3,424	1,069	12,152	13,627	7,881	8,992	4,271	4,635	0.351	0.340 0.343	6,705	6,892	3,590	3,590 3,580	3,115	3,302	0.465	0.479
2014/04/21 2014/04/28	3,428 3,419	1,075	12,351 12,942	13,453 13,965	7,956 8,419	8,838 9,279	4,396	4,615 4,686	0.356	0.345	6,751 6,890	6,880 6,982	3,580 3,659	3,580	3,171 3,231	3,300 3,323	0.470	0.480 0.476
2014/05/05	3,468	1,075	13,039	13,559	8,402	8,965	4,637	4,594	0.356	0.339	6,899	6,893	3,625	3,625	3,274	3,268	0.475	0.474
2014/05/12 2014/05/19	3,476 3,479	1,074 1,077	12,599 13,298	13,387 14,269	8,077 8,527	8,812 9,412	4,522 4,771	4,575 4,857	0.359	0.342 0.340	6,832 6,945	6,865 6,974	3,576 3,644	3,576	3,256 3,301	3,289 3,330	0.477 0.475	0.479 0.477
2014/05/26	3,479	1,077	13,298	13,797	8,527	9,412 9,114	4,908	4,682	0.359	0.340	6,970	6,926	3,644	3,644 3,633	3,301	3,330	0.473	
2014/06/02	3,479	1,079	13,258	14,031	8,444	9,229	4,814	4,801	0.363	0.342	6,914	6,935	3,609	3,609	3,305	3,326	0.478	0.480
2014/06/09 2014/06/16	3,486 3,473	1,078	14,055 13,337	14,662 13,781	8,982 8,483	9,721 9,063	5,072 4,854	4,941 4,718	0.361 0.364	0.337 0.342	7,104 6,966	7,059 6,919	3,705 3,612	3,705 3,612	3,399 3,354	3,354 3,307	0.478 0.481	0.475 0.478
2014/06/23	3,482	1,032	13,787	14,511	8,858	9,580	4,929	4,932	0.358	0.340	7,042	7,068	3,688	3,688	3,355	3,381	0.431	0.478
2014/06/30	3,491	1,080	13,826	14,366	8,856	9,489	4,970	4,877	0.359	0.339	7,051	6,992	3,664	3,664	3,387	3,328	0.480	0.476
2014/07/07 2014/07/14	3,491 3,486	1,083	13,666 13,622	14,611 14,547	8,732 8,699	9,655 9,634	4,934 4,922	4,956 4,913	0.361 0.361	0.339 0.338	7,000 6,974	6,944 6,953	3,621 3,625	3,621 3,625	3,379 3,348	3,323 3,327	0.483 0.480	0.479 0.479
2014/07/21	3,488	1,080	14,563	14,381	9,316	9,572	5,247	4,809	0.360	0.334	7,034	6,909	3,636	3,636	3,398	3,273	0.483	0.474
2014/07/28	3,486	1,078	14,148	14,410	9,131	9,600	5,017	4,809	0.355	0.334	6,978	6,931	3,635	3,635	3,343	3,296	0.479	0.476
2014/08/04 2014/08/11	3,517 3,478	1,081	13,974 14,674	15,113	9,054 9,613	10,132 10,460	4,920 5,061	4,981 4,924	0.352	0.330	6,997 7,104	6,988 6,990	3,656 3,705	3,656 3,705	3,341 3,398	3,333 3,285	0.477	0.477 0.470
2014/08/18	3,499	1,080	13,578	14,337	8,706	9,510	4,872	4,827	0.359	0.337	6,958	6,912	3,621	3,621	3,338	3,291	0.480	0.476
2014/08/25 2014/09/01	3,494 3,511	1,079 1,075	13,556 13,325	14,041	8,671 8,491	9,328 8,927	4,885 4,835	4,712 4,549	0.360	0.336 0.338	7,008 6,978	6,901 6,886	3,639 3,597	3,639 3,597	3,370 3,381	3,262 3,289	0.481 0.485	0.473 0.478
2014/09/01 2014/09/08	3,511	1,075	13,325	13,477 13,565	8,491 8,211	8,927	4,835	4,549	0.365	0.338	6,978	6,880	3,597	3,597	3,360	3,289	0.485	0.478
2014/09/15	3,508	1,080	13,274	13,619	8,481	9,033	4,793	4,586	0.361	0.337	7,029	6,919	3,624	3,624	3,405	3,295	0.484	0.476
2014/09/22 2014/09/29	3,510 3,507	1,067 1,071	13,481 13,359	14,020 13,204	8,637 8,579	9,275 8,613	4,844 4,780	4,745 4,590	0.359 0.358	0.338 0.348	7,055	7,027 6,999	3,672 3,667	3,672 3,667	3,383 3,396	3,355 3,332	0.479 0.481	0.477
2014/09/29	3,507	1,071	13,339	12,684	8,509	8,197	4,780	4,390	0.358	0.348	7,003	6,979	3,656	3,656	3,390	3,332	0.481	0.476
2014/10/13	3,518	1,063	13,107	13,265	8,419	8,649	4,688	4,616	0.358	0.348	7,125	7,083	3,706	3,706	3,420	3,378	0.480	0.477
2014/10/20 2014/10/27	3,519 3,519	1,070 1,073	13,584 13,066	13,343 12,685	8,700 8,407	8,763 8,218	4,884 4,660	4,579 4,467	0.360	0.343 0.352	7,166 7,105	7,066 7,047	3,710 3,684	3,710 3,684	3,456 3,421	3,355 3,363	0.482 0.482	0.475
2014/10/27 2014/11/03	3,319	1,073	13,000	12,085	8,395	8,467	4,600	4,407	0.357	0.332	7,103	7,047	3,689	3,689	3,421	3,303	0.482	0.477
2014/11/10	3,514	1,068	12,944	12,682	8,332	8,335	4,612	4,348	0.356	0.343	7,122	7,018	3,686	3,686	3,435	3,332	0.482	0.475
2014/11/17 2014/11/24	3,513 3,514	1,069	12,909 13,410	12,686	8,261 8,650	8,092 8,762	4,647 4,759	4,594 4,580	0.360	0.362	7,067	7,022 7,091	3,660 3,717	3,660 3,717	3,407 3,437	3,362 3,374	0.482	0.479 0.476
2014/11/24 2014/12/01	3,514	1,072	13,410	13,343	8,763	8,702 8,591	4,739	4,580	0.355	0.343	7,133	7,091	3,734	3,734	3,437	3,374	0.480	0.476
2014/12/08	3,538	1,071	13,726	13,448	8,944	8,810	4,783	4,638	0.348	0.345	7,286	7,221	3,805	3,805	3,481	3,416	0.478	0.473
2014/12/15 2014/12/22	3,539 3,543	1,069	14,253 15,823	13,242 15,281	9,361 10,703	8,771 10,317	4,892 5,120	4,471 4,964	0.343	0.338	7,356 7,573	7,186 7,523	3,836 4,070	3,836 4,070	3,520 3,504	3,350 3,454	0.478	0.466 0.459
2014/12/22	3,343	1,075	13,823	14,212	9,739	9,928	4,710	4,904	0.324	0.323	7,086	6,955	3,713	3,713	3,304	3,434	0.403	0.439

Table 1: Summary of the Dataset

Notes: Weekly information about sales and the number of items in all, continuing goods, new goods, and disappearing goods.

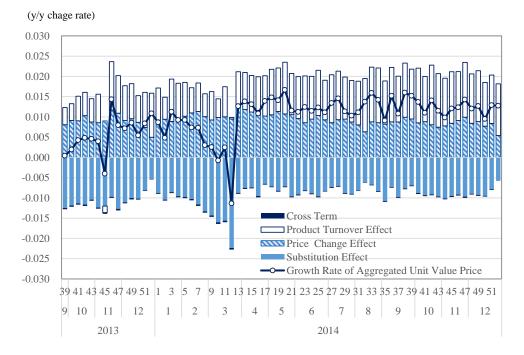
4. Movements in Price Index and Its Decomposition

4.1 The Aggregate Index

Figure 3 shows movements in the rate of change in the unit price index and its decomposition into the three effects. Before interpreting Figure 3, we again note that on April 1, 2014, Japan's consumption tax rate increased from 5% to 8%, first major change since 1997.¹² Although the dataset used in this paper is pre-tax, we expect to see discontinuous changes before and after April 1, 2014.

From Figure 3, we observe that in most periods, turnover-new product effects are positive, a finding consistent with the case in Figure 2. This implies that the prices of new goods exceed the prices of continuing goods or that the prices of continuing goods exceed the prices of disappearing goods. The magnitude of the contribution of the turnover-new goods effects was about 1.5 percentage points. This figure is much larger than the estimates by Boskin et al. (1996), which indicated that the introduction of new and better products added 0.6 of a percentage point to annual consumption growth in the United States.

On the other hand, the substitution effects—i.e., the effects of the shift in demand from higher to lower priced products—are negative, implying that consumers increase expenditures on lower-priced goods. Compared with other price effects, the magnitude of the cross term is negligible.





Notes: Unit Value Price corresponds to Equation (12). The three types of bars correspond to the contributions of three

¹² Scanner data used in this study exclude consumption taxes. That is, price information in the dataset is pre-tax.

price effects in Equations (13) - (15).

During our sampled period, the unit value price index exhibited large ups and downs in mid-November 2013. This turbulence occurred resulted from different dates for the Beaujolais Nouveau Day.¹³ From January until the end of March in 2014, the unit value price index declined, and then, it skyrocketed in the week that includes April 1, 2014. Compared with the large fluctuation in the unit value price index, the standard price change effects are quite stable. This implies that the frequency and/or magnitude of product-level price changes did not significantly vary during the sampled periods. The decline in the unit value price index during the first quarter in 2014 came with increasing substitution effects. Behind the dramatic decline in the substitution effect, there is a surge in total expenditures before the tax revision. Figure 4 shows that total sales surged by 20–30% just before the change in tax rate. We summarise that expecting consumers anticipated the tax increase and stockpiled lower-priced commodities, thereby increasing the substitution effects.

After the tax increase, the turnover-new goods effects surpass those evident before the tax revision, which contributed to the increase in the unit value price index. From Figure 4 we observe that the rate of sales growth for new goods exceeded that of continuing goods, suggesting an increasing economic role for new goods after the tax revision. After June, 2014, the contribution of the turnover-new goods effects became the largest of the three factors, implying relatively higher prices for new goods (Figure 3). Those facts suggest that introducing new goods is an instrument to increase product prices.

¹³ Beaujolais Nouveau Day is the third Thursday of November. In 2012, the third Thursday fell on November 15 during the second week of month, and in 2013, it fell on November 21 during the third week. When calculating the rates of change, we take differences from the same week in the previous year, for differences in dates of important events can strongly affect unit prices. Because Beaujolais Nouveau generally costs more than other average wines, unit prices during the second week of November 2013 were much lower than during the second week in November 2012. That circumstances caused huge ups and downs in the aggregate unit value price index in Figure 3.

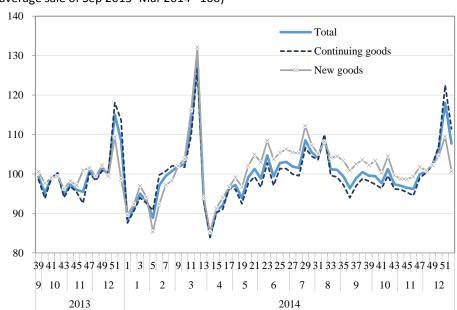
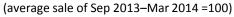


Figure 4: Movements in Total Sales and Sales of New Goods



Notes: This figure is based on sales information in Table 1.

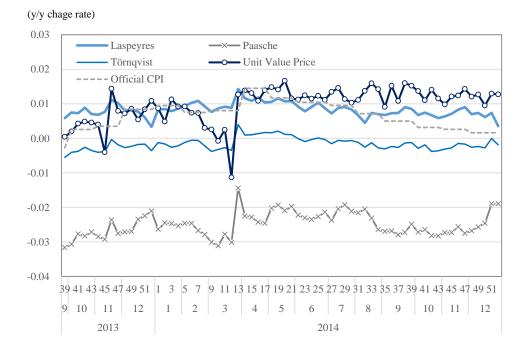


Figure 5: Comparisons of Several Price Indexes

Notes: Unit Value Price is identical to that in Figure 3. See Appendix 3 for details of the Laspeyres, Paasche, and Törnqvist indexes. When plotting the official CPI, we first chose 115 product categories that overlap those categories in the SRI with volume information. Then, we aggregated the category-level official CPIs to obtain the aggregate official CPI depicted in Figure 5.

Figure 5 compares the unit value price index to the standard price indexes: Laspeyres, Paasche, and Törnqvist indexes and the Japanese official CPI based on 115 product categories that overlap with SRI.¹⁴ First, it is significant that the discrepancy between Laspeyres and Paasche indexes is large. The Paasche index moves from -3% to -2%, while the Laspeyres index moves from 0% to 1%. One main cause of this departure is bargain sales. When commodities go on bargain sale, prices decline, sales quantities surge, and the weights of the commodities in the Paasche index are increased. Bargain sales in the current period do not change the weights in the Laspeyres index because they are by definition unchanged in the Laspeyres index.

The official CPI that is also constructed by Laspeyres formula tracks our Laspeyres index closely except for August–December 2014.¹⁵ This similarity indicates that factors excluded in the official CPI, such as bargain sales and substation from higher to lower priced goods might not affect the general price level during the sampled period as long as we use the weight at base periods.

The unit value price index exhibits a generally higher rate of change than the Törnqvist index.¹⁶ The huge departure between the Törnqvist index based only on continuing goods and the unit value price index based on all traded goods implies significant roles for (1) the price differential between new and continuing goods and (2) substitution effects. For example, before the tax revision, the unit value price index declined, but the Törnqvist index was stable. Figure 3 reveals that, during the period, the substitution effects become larger than those in other periods.

4.2. Movements in Several Commodity Categories

This subsection analyzes the movements in the unit price index and its decomposition at the category level. Contributions of the three effects on the unit value price index vary across product categories to a large extent.

¹⁴ See Appendix 3 for the formula used to calculate these price indexes. The Fisher index exhibits movements almost identical to the Törnqvist index; hence, we exclude it from Figure 5.

¹⁵ The main differences between the official CPI and our Laspeyres index are as follows: (1) items adopted in the official CPI are one or a few popular products for each category, whereas SRI covers all products, (2) the official CPI does not incorporate information for bargain sales, whereas SRI includes sales and price information at bargain sales, and (3) the official CPI uses prices from the largest retailers for each region, whereas SRI contains different types of stores such as convenience stores, supermarkets, and general merchandise stores.

¹⁶ Note that we use the Törnqvist formula when aggregating categorical unit value price indexes.

Figures 6 and 7 depict movements of several price indexes and the unit value price decomposition of heavy detergent and yogurt. The Törnqvist indexes exhibit very similar movements to those of the official CPI. After the tax revision, both goods exhibit very large positive turnover-new goods effects, which resulted in large discrepancies between the unit value price index and the official CPI.

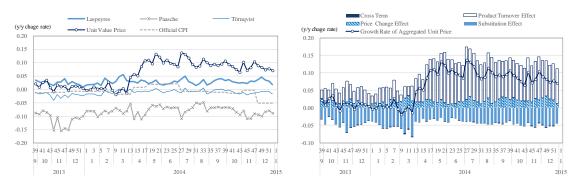


Figure 6: Decomposition of Unit Price Index (Heavy Detergent)

Notes: See the notes for Figures 3 and 5 for details except for the official CPI.

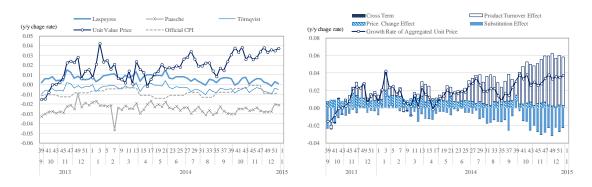


Figure 7: Decomposition of Unit Price Index (Yogurt)

Figures 8 and 9 exhibit the cases of butter and facial tissues. Butter shows a rising trend, whereas facial tissues show a declining price trend. Contributions from the turnover-new goods effects and the substitution effects are minor in these cases. Most changes in the unit value price index come from changes in the product price change (π_t^{CL}). Thus, the unit value price indexes track the official CPIs very closely.

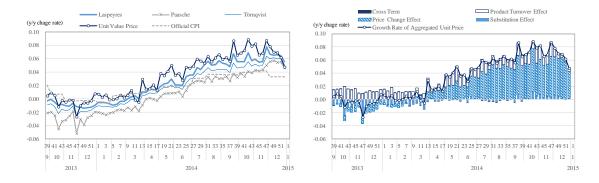
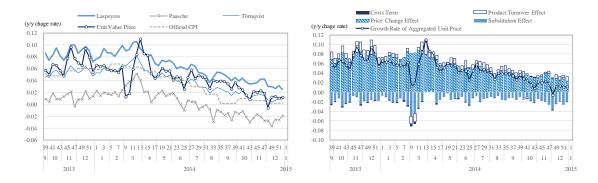
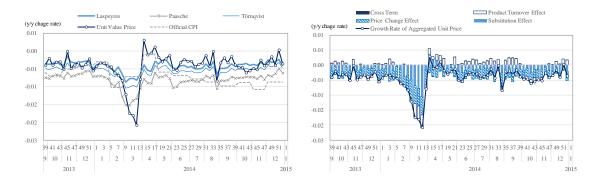


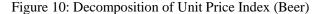
Figure 8: Decomposition of Unit Price Index (Butter)

Figure 9: Decomposition of Unit Price Index (Facial Tissue)



Finally, Figures 10 and 11 present the cases of beer and salt. Both goods exhibit strong negative substitution effects just before the tax revision, whereas the turnover-new goods effects are moderate. Overall, the unit price of a case of beer (24 cans) is much lower than the price of the same beer sold separately. Similarly, the unit price of 1 kilogram of salt is much lower than that of 100 grams of the same salt sold as cooking salt. Both goods can be stored a long time. Thus, before the tax increase, consumers likely stockpiled those goods, reducing the unit value price index during the period.





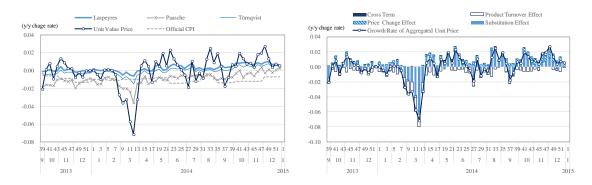


Figure 11: Decomposition of Unit Price Index (Salt)

5. Conclusion

This study has investigated unit price indexes based on large-scale retail scanner data. By extending the technique developed by Silver (2009, 2010) and Diewert and Lippe (2010), we decomposed changes in unit price into (1) turnover–new goods effects, (2) substitution effects, and (3) price change effects (Laspeyres price index). The aggregate unit value price index shows a higher rate of inflation than other price indexes, such as the Törnqvist index. Product turnover effects are generally positive, implying that new products are priced higher than disappearing or continuing goods. Substitution effects are generally negative, implying that negative correlation between volume shares and prices. Substitution effects strengthened just before the tax revision, likely reflecting consumer stockpiling behaviors, which reduced the unit value price inflation to a large extent. As measured by the Laspeyres formula, (pre-tax) commodity prices were scarcely changed before or after the tax revision, which implies that the patterns of product-level commodity price change were unchanged. After the tax rate increase, the turnover-new product effects increased by 1 percentage point, contributing to the increase in unit value prices.

Category-level analyses revealed that the influence of the three effects on the unit value price index varies greatly across product categories. Unit value price indexes exhibit movements similar to the official CPI for some goods with few turnover-new goods effects evident in such items as butter and facial tissue. However, some goods with large turnover-new goods effects such as heavy detergent and yogurt exhibit large discrepancies between unit value price indexes and official CPIs.

Many tasks related to our work remain. The increasing share of sales of new goods after the tax revision implies that the introduction of new goods to a certain extent is instrumental for price adjustment. The increase in the unit value price index after the tax revision was mainly caused by the introduction of high-priced new goods. If such factors as potential damage to product brands prevent producers from changing prices, introducing slightly different new goods can be more profitable than simply adjusting prices. Micro-analyses of price and product adjustments merit further investigation.

This study did not consider changes product quality such as taste or durability. In general, quality of processed foods and daily necessities is very difficult to measure. The Statistics Bureau of Japan does not adjust for quality of processed foods and daily necessities, except for volume (change in gram or milliliter), when constructing its consumer price index. Given that the information about characteristics, except for volume, is scarce for processed foods and daily necessities, it is difficult to employ a hedonic approach. If quality of new products surpasses that of incumbent goods, this study's estimates of unit price are vulnerable to upward bias. More detailed categorical-level investigations are needed to address the quality issue.

Other remaining tasks include the analysis of (1) the effects of the tax rate on the cycle of products introduced just before the tax reform, (2) possible measures for the cost of living index, such as the multilateral chained index proposed by De Haan and Van der Grient (2011), and (3) the impact on commodity prices of the large depreciation in the Japanese yen.

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Appendix 1: Derivation of Covariance Expression for the Substitution Effects:

Define

,

$$Cov(x,y) = \frac{1}{T} \sum_{i} (x_i - x^*)(y_i - y^*) = \frac{1}{T} \sum_{i} (x_i)(y_i - y^*),$$

where
$$s_t^i = \frac{q_t^i}{\sum_{j \in C_t} q_t^j}$$
,
 $p_t = [p_t^1, p_t^2, \dots, p_t^{T_t}]$,
 $s_t = [s_t^1, s_t^2, \dots, s_t^{T_t}]$,

 T_t : #(Θ_t), the number of products sold at time *t*.

The substitution effects (ϕ_t^C) can be transformed as follows,

$$\phi_t^C \equiv \frac{P_t^C - \ddot{P}_t^C}{P_t^C} = \frac{\sum_{i \in C_t} p_t^i \left[\frac{q_t^i}{\sum_{j \in C_t} q_t^j} - \frac{q_{t-y}^i}{\sum_{j \in C_t} q_{t-y}^j} \right]}{\sum_{i \in C_t} \left[\frac{q_t^i}{\sum_{j \in C_t} q_t^j} \times p_t^i \right]}$$
$$= \frac{\sum_{i \in C_t} p_t^i [s_t^i - s_{t-y}^i]}{\sum_{i \in C_t} \left[\frac{q_t^i}{\sum_{j \in C_t} q_t^j} \times p_t^i \right]}$$

Because s_t^i and s_{t-y}^i are volume shares of good *i*, in times *t* and *t*-*y*, their averages are the same. That is, $\sum_{i \in C_t} [s_t^i - s_{t-y}^i] = 0.$

Thus, we can obtain,

$$\sum_{i\in c_t} p_t^i [s_t^i - s_{t-y}^i] = T_t \operatorname{Cov}(p_t, s_t - s_{t-y}).$$

•

Therefore, the substitution effects can be written by this covariance:

$$\phi_t^C = \frac{T_t \operatorname{Cov}(p_t, s_t - s_{t-y})}{P_t^C}.$$

Appendix 2: Derivation of the Unit Value Price Decomposition

$$\begin{aligned} \pi_{t}^{\Theta} &= \left(\frac{P_{t-y}^{C}}{P_{t-y}^{\Theta}}\right) w_{t-y}^{C} \pi_{t}^{CL} + \left(\frac{P_{t-y}^{C}}{P_{t-y}^{\Theta}}\right) w_{t-y}^{C} \tilde{\pi}_{t}^{C} + \left(\frac{P_{t-y}^{O}}{P_{t-y}^{\Theta}}\right) w_{t-y}^{O} \tilde{\pi}_{t}^{T} \\ &= \left(\frac{P_{t-y}^{C}}{P_{t-y}^{\Theta}}\right) w_{t-y}^{CL} + \left(\frac{P_{t-y}^{C}}{P_{t-y}^{\Theta}}\right) w_{t-y}^{C} \{ \left(w_{t}^{C} / w_{t-y}^{C} - 1\right) + \phi_{t}^{C} + \left(w_{t}^{C} / w_{t-y}^{C} - 1\right) \pi_{t}^{C} + \phi_{t}^{C} \pi_{t}^{C} \} \\ &+ \left(\frac{P_{t-y}^{O}}{P_{t-y}^{\Theta}}\right) w_{t-y}^{O} \{ \left(w_{t}^{N} / w_{t-y}^{O} - 1\right) + \pi_{t}^{NO} + \left(w_{t}^{N} / w_{t-y}^{O} - 1\right) \pi_{t}^{NO} \} \end{aligned}$$

$$= \left(\frac{P_{t-y}^{C}}{P_{t-y}^{\Theta}}\right) w_{t-y}^{C} \pi_{t}^{CL} + \left(\frac{P_{t-y}^{O}}{P_{t-y}^{O}}\right) w_{t-y}^{C} \phi_{t}^{C} + \left(\frac{P_{t-y}^{O}}{P_{t-y}^{O}}\right) w_{t-y}^{O} \pi_{t}^{NO} + \left(\frac{P_{t-y}^{C}}{P_{t-y}^{O}}\right) \left(w_{t}^{C} - w_{t-y}^{C}\right) \pi_{t}^{C} \\ &+ \left(\frac{P_{t-y}^{O}}{P_{t-y}^{O}}\right) \left(w_{t}^{N} - w_{t-y}^{O}\right) \pi_{t}^{NO} + \left(\frac{P_{t-y}^{O} - P_{t-y}^{C}}{P_{t-y}^{O}}\right) \left(w_{t}^{N} - w_{t-y}^{O}\right) + \left(\frac{P_{t-y}^{C}}{P_{t-y}^{O}}\right) w_{t-y}^{C} \phi_{t}^{C} \pi_{t}^{C} , \\ &\text{where } \pi_{t}^{C} \equiv \frac{P_{t}^{C} - P_{t-y}^{C}}{P_{t-y}^{C}}, \ \phi_{t}^{C} \equiv \frac{P_{t}^{C} - P_{t-y}^{C}}{P_{t-y}^{C}}, \ \text{and}, \ \pi_{t}^{NO} \equiv \frac{P_{t}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}. \end{aligned}$$

Arrangement of Turnover Effect Terms:

Note that $w_t^C - w_{t-y}^C = 1 - w_t^N - (1 - w_{t-y}^O) = -(w_t^N - w_{t-y}^O).$

The turnover effect term can be greatly simplified as follows,

$$\begin{split} & \left(\frac{P_{t-y}^{O}}{P_{t-y}^{\Theta}}\right) w_{t-y}^{O} \pi_{t}^{NO} + \left(\frac{P_{t-y}^{C}}{P_{t-y}^{\Theta}}\right) \left(w_{t}^{C} - w_{t-y}^{C}\right) \pi_{t}^{C} + \left(\frac{P_{t-y}^{O}}{P_{t-y}^{\Theta}}\right) \left(w_{t}^{N} - w_{t-y}^{O}\right) \pi_{t}^{NO} \\ & \quad + \left(\frac{P_{t-y}^{O} - P_{t-y}^{C}}{P_{t-y}^{O}}\right) \left(w_{t}^{N} - w_{t-y}^{O}\right) \\ & \quad = \left(\frac{P_{t-y}^{O}}{P_{t-y}^{O}}\right) w_{t-y}^{O} \left(\frac{P_{t}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}\right) + \left(\frac{P_{t-y}^{C}}{P_{t-y}^{O}}\right) \left(w_{t}^{C} - w_{t-y}^{C}\right) \left(\frac{P_{t}^{C} - P_{t-y}^{C}}{P_{t-y}^{O}}\right) \\ & \quad + \left(\frac{P_{t-y}^{O}}{P_{t-y}^{O}}\right) \left(w_{t}^{N} - w_{t-y}^{O}\right) \left(\frac{P_{t}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}\right) + \left(\frac{P_{t-y}^{O} - P_{t-y}^{C}}{P_{t-y}^{O}}\right) \left(w_{t}^{N} - w_{t-y}^{O}\right) \\ & \quad = \left(\frac{P_{t}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}\right) w_{t-y}^{O} + \left(\frac{P_{t}^{C} - P_{t-y}^{C}}{P_{t-y}^{O}}\right) \left(w_{t}^{C} - w_{t-y}^{C}\right) + \left(\frac{P_{t-y}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}\right) \left(w_{t}^{N} - w_{t-y}^{O}\right) \\ & \quad + \left(\frac{P_{t-y}^{O} - P_{t-y}^{C}}{P_{t-y}^{O}}\right) \left(w_{t}^{N} - w_{t-y}^{O}\right) \\ & \quad = \left(\frac{P_{t}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}\right) w_{t-y}^{O} + \left(\frac{-\left(P_{t}^{C} - P_{t-y}^{C}\right) + \left(P_{t}^{N} - P_{t-y}^{O}\right) + \left(P_{t-y}^{O} - P_{t-y}^{C}\right)}{P_{t-y}^{O}}\right) \left(w_{t}^{N} - w_{t-y}^{O}\right) \\ & \quad = \left(\frac{P_{t}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}\right) w_{t-y}^{O} + \left(\frac{-\left(P_{t}^{C} - P_{t-y}^{C}\right) + \left(P_{t-y}^{N} - P_{t-y}^{O}\right) + \left(P_{t-y}^{O} - P_{t-y}^{C}\right)}{P_{t-y}^{O}}\right) \left(w_{t}^{N} - w_{t-y}^{O}\right) \\ & \quad = \left(\frac{P_{t}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}\right) w_{t-y}^{O} + \left(\frac{-\left(P_{t}^{C} - P_{t-y}^{C}\right) + \left(P_{t-y}^{N} - P_{t-y}^{O}\right) + \left(P_{t-y}^{O} - P_{t-y}^{O}\right)}{P_{t-y}^{O}}\right) \left(w_{t}^{N} - w_{t-y}^{O}\right) \\ & \quad = \left(\frac{P_{t}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}\right) w_{t-y}^{O} + \left(\frac{-\left(P_{t}^{C} - P_{t-y}^{C}\right) + \left(P_{t-y}^{O} - P_{t-y}^{O}\right) + \left(P_{t-y}^{O} - P_{t-y}^{O}\right)}{P_{t-y}^{O}}\right) \left(w_{t}^{N} - w_{t-y}^{O}\right) \\ & \quad = \left(\frac{P_{t}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}\right) w_{t-y}^{O} + \left(\frac{-\left(P_{t-y}^{O} - P_{t-y}^{O}\right) + \left(P_{t-y}^{O} - P_{t-y}^{O}\right) + \left(P_{t-y}^{O} - P_{t-y}^{O}\right)}{P_{t-y}^{O}}\right) \\ & \quad = \left(\frac{P_{t}^{N} - P_{t-y}^{O}}{P_{t-y}^{O}}\right) w_{t-y}^{O} +$$

$$= \frac{w_{t-y}^{O}(P_{t}^{N} - P_{t-y}^{O}) + (w_{t}^{N} - w_{t-y}^{O})(P_{t}^{N} - P_{t}^{C})}{P_{t-y}^{\Theta}}$$
$$= \frac{w_{t-y}^{O}(P_{t}^{C} - P_{t-y}^{O}) + w_{t}^{N}(P_{t}^{N} - P_{t}^{C})}{P_{t-y}^{\Theta}}$$

Appendix 3: Formula for Price Indixes

Laspeyres, Paasche, and Törnqvist indexes depicted in Figure 5 are obtained using the following formula:

Laspeyres index inflation rate:

$$\begin{split} \pi_t^{CL} &= \frac{\sum_{i \in C_t} [q_{t-y}^i p_t^i]}{\sum_{i \in C_t} [q_{t-y}^i p_{t-y}^i]} - \frac{\sum_{i \in C_t} [q_{t-y}^i p_{t-y}^i]}{\sum_{i \in C_t} [q_{t-y}^i p_{t-y}^i]} \\ &= \sum_{i \in C_t} \left[\frac{q_{t-y}^i p_{t-y}^i}{\sum_{i \in C_t} [q_{t-y}^i p_{t-y}^i]} \left(\frac{p_t^i}{p_{t-y}^i} \right) \right] - \sum_{i \in C_t} \left[\frac{q_{t-y}^i p_{t-y}^i}{\sum_{i \in C_t} [q_{t-y}^i p_{t-y}^i]} \left(\frac{p_{t-y}^i}{p_{t-y}^i} \right) \right] \\ &= \sum_{i \in C_t} \left[\frac{q_{t-y}^i p_{t-y}^i}{\sum_{i \in C_t} [q_{t-y}^i p_{t-y}^i]} \left(\frac{p_{t-y}^i p_{t-y}^i}{p_{t-y}^i} \right) \right] \right]. \end{split}$$

> The Paasche index inflation rate:

$$\pi_t^{CP} = \frac{\sum_{i \in C_t} [q_t^i p_t^i]}{\sum_{i \in C_t} [q_t^i p_{t-y}^i]} - 1 = \frac{1}{\frac{\sum_{i \in C_t} [q_t^i p_{t-y}^i]}{\sum_{i \in C_t} [q_t^i p_t^i]}} - 1 = \frac{1}{\sum_{i \in C_t} \left[\frac{q_t^i p_t^i}{\sum_{i \in C_t} [q_t^i p_t^i]} \left(\frac{p_{t-y}^i}{p_t^i}\right)\right]} - 1.$$

> The Törnqvist index inflation rate:

$$\pi_t^{Tq} = \exp\left\{\sum_{i\in C_t} \left[\frac{1}{2} \left(\frac{q_{t-y}^i p_{t-y}^i}{\sum_{i\in C_t} [q_{t-y}^i p_{t-y}^i]} + \frac{q_t^i p_t^i}{\sum_{i\in C_t} [q_t^i p_t^i]}\right) \ln\left(\frac{p_t^i}{p_{t-y}^i}\right)\right]\right\} - 1.$$